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**香港考試及評核局**  
**HONG KONG EXAMINATIONS AND ASSESSMENT AUTHORITY**

**2022年香港中學文憑考試**  
**HONG KONG DIPLOMA OF SECONDARY EDUCATION EXAMINATION 2022**

**數學                      必修部分                      試卷一**  
**MATHEMATICS    COMPULSORY PART    PAPER 1**

**評卷參考**  
**MARKING SCHEME**

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**Hong Kong Diploma of Secondary Education Examination**  
**Mathematics Compulsory Part Paper 1**

**General Marking Instructions**

1. It is very important that all markers should adhere as closely as possible to the marking scheme. In many cases, however, candidates will have obtained a correct answer by an alternative method not specified in the marking scheme. In general, a correct answer merits ***all the marks*** allocated to that part, unless a particular method has been specified in the question. Markers should be patient in marking alternative solutions not specified in the marking scheme.
2. In the marking scheme, marks are classified into the following three categories:

|                          |                                                                                        |
|--------------------------|----------------------------------------------------------------------------------------|
| ‘M’ marks                | awarded for correct methods being used;                                                |
| ‘A’ marks                | awarded for the accuracy of the answers;                                               |
| Marks without ‘M’ or ‘A’ | awarded for correctly completing a proof or arriving at an answer given in a question. |

In a question consisting of several parts each depending on the previous parts, ‘M’ marks should be awarded to steps or methods correctly deduced from previous answers, even if these answers are erroneous. However, ‘A’ marks for the corresponding answers should NOT be awarded (unless otherwise specified).
3. For the convenience of markers, the marking scheme was written as detailed as possible. However, it is still likely that candidates would not present their solution in the same explicit manner, e.g. some steps would either be omitted or stated implicitly. In such cases, markers should exercise their discretion in marking candidates’ work. In general, marks for a certain step should be awarded if candidates’ solution indicated that the relevant concept/technique had been used.
4. In marking candidates’ work, the benefit of doubt should be given in the candidates’ favour.
5. In the marking scheme, ‘r.t.’ stands for ‘accepting answers which can be rounded off to’ and ‘f.t.’ stands for ‘follow through’. Steps which can be skipped are shaded whereas alternative answers are enclosed with rectangles. All fractional answers must be simplified.

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| Solution                                                                                                                                                                                                       | Marks                                                    | Remarks                                                                                                                                                            |
|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <p>1. <math>\frac{(a^3b^{-2})^4}{a^{-5}b^6}</math></p> $= \frac{a^{12}b^{-8}}{a^{-5}b^6}$ $= \frac{a^{12+5}}{b^{6+8}}$ $= \frac{a^{17}}{b^{14}}$                                                               | <p>1M</p> <p>1M</p> <p>1A</p> <p>----- (3)</p>           | <p>for <math>(m^h)^k = m^{hk}</math> or <math>(mn)^l = m^l n^l</math></p> <p>for <math>\frac{x^p}{x^q} = x^{p-q}</math> or <math>y^{-r} = \frac{1}{y^r}</math></p> |
| <p>2. Note that <math>x + y = 456</math> and <math>7x = y</math>.</p> <p>So, we have <math>x + 7x = 456</math>.</p> <p>Solving, we have <math>x = 57</math>.</p>                                               | <p>1A</p> <p>1M</p> <p>1A</p>                            | <p>for either correct</p> <p>for getting a linear equation in <math>x</math> or <math>y</math> only</p>                                                            |
| $\frac{x}{456}$ $= \frac{1}{1+7}$ $= 57$                                                                                                                                                                       | <p>1M+1A</p> <p>1A</p> <p>----- (3)</p>                  | <p>1M for fraction</p>                                                                                                                                             |
| <p>3. <math>\frac{3}{k-9} + \frac{2}{5k+6}</math></p> $= \frac{3(5k+6) + 2(k-9)}{(k-9)(5k+6)}$ $= \frac{15k+18+2k-18}{(k-9)(5k+6)}$ $= \frac{17k}{(k-9)(5k+6)}$                                                | <p>1M</p> <p>1M</p> <p>1A</p> <p>----- (3)</p>           | <p>or equivalent</p>                                                                                                                                               |
| <p>4. (a) <math>9c^2 - 6c + 1</math></p> $= (3c-1)^2$ <p>(b) <math>(4c+d)^2 - 9c^2 + 6c - 1</math></p> $= (4c+d)^2 - (9c^2 - 6c + 1)$ $= (4c+d)^2 - (3c-1)^2$ $= (4c+d+3c-1)(4c+d-(3c-1))$ $= (7c+d-1)(c+d+1)$ | <p>1A</p> <p>1M</p> <p>1M</p> <p>1A</p> <p>----- (4)</p> | <p>or equivalent</p> <p>for using the result of (a)</p> <p>or equivalent</p>                                                                                       |

| Solution                                                                                                                                                                                                                                                                                                   | Marks                                   | Remarks                                                          |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------|------------------------------------------------------------------|
| <p>5. Let \$ x be the cost of the fan.</p> $(26\%)x = 78$ $x = \frac{78}{0.26}$ $x = 300$ <p>The selling price of the fan</p> $= 300 + 78$ $= \$ 378$ <p>Let \$ y be the marked price of the fan.</p> $(70\%)y = 378$ $y = \frac{378}{0.7}$ $y = 540$ <p>Thus, the marked price of the fan is \$ 540 .</p> | <p>1M</p> <p>1M</p> <p>1M</p> <p>1A</p> |                                                                  |
| <p>The marked price of the fan</p> $= \frac{(78)(1+26\%)}{(26\%)(70\%)}$ $= \$ 540$                                                                                                                                                                                                                        | <p>1M+1M+1M</p> <p>1A</p>               | <p>{ 1M for fraction + 1M for numerator + 1M for denominator</p> |
| ----- (4)                                                                                                                                                                                                                                                                                                  |                                         |                                                                  |
| <p>6. (a) <math>-2(3x+2) &gt; x+10</math></p> $-6x-4 > x+10$ $-6x-x > 10+4$ $-7x > 14$ $x < -2$<br>$2x \leq -8$ $x \leq -4$ <p>Therefore, we have <math>x &lt; -2</math> or <math>x \leq -4</math> .</p> <p>Thus, the solution of (*) is <math>x &lt; -2</math> .</p>                                      | <p>1M</p> <p>1A</p> <p>1A</p>           | <p>for putting <math>x</math> on one side</p>                    |
| <p>(b) <math>-3</math></p>                                                                                                                                                                                                                                                                                 | <p>1A</p>                               |                                                                  |
| ----- (4)                                                                                                                                                                                                                                                                                                  |                                         |                                                                  |
| <p>7. (a) The coordinates of <math>S'</math> are <math>(5, 12)</math> .</p> <p>The coordinates of <math>T'</math> are <math>(-3, 7)</math> .</p>                                                                                                                                                           | <p>1A</p> <p>1A</p>                     |                                                                  |
| <p>(b) The slope of <math>S'T'</math></p> $= \frac{12-7}{5-(-3)}$ $= \frac{5}{8}$                                                                                                                                                                                                                          | <p>1M</p> <p>1A</p>                     | <p>0.625</p>                                                     |
| ----- (4)                                                                                                                                                                                                                                                                                                  |                                         |                                                                  |

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2022-DSE-MATH-CP 1-5

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| Solution                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | Marks                                         | Remarks                                                                         |
|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------|---------------------------------------------------------------------------------|
| <p>10. (a) Let <math>f(x) = ax^2 + bx</math>, where <math>a</math> and <math>b</math> are non-zero constants.<br/>           So, we have <math>16a + 4b = 96</math> and <math>25a - 5b = 15</math>.<br/>           Solving, we have <math>a = 3</math> and <math>b = 12</math>.<br/>           Thus, we have <math>f(x) = 3x^2 + 12x</math>.</p>                                                                                                                                                                | <p>1A<br/>1M<br/>1A</p> <p>----- (3)</p>      | <p>for either substitution<br/>for both correct</p>                             |
| <p>(b) The <math>x</math>-intercepts of the graph of <math>y = 8f(x)</math> are 0 and <math>-4</math>.</p>                                                                                                                                                                                                                                                                                                                                                                                                      | <p>1A</p> <p>----- (1)</p>                    | <p>for both correct</p>                                                         |
| <p>(c) The equation <math>3x^2 + 12x - k = 0</math> has two distinct real roots.<br/> <math>12^2 - 4(3)(-k) &gt; 0</math><br/> <math>k &gt; -12</math></p>                                                                                                                                                                                                                                                                                                                                                      | <p>1M<br/>1A</p> <p>----- (2)</p>             |                                                                                 |
| <p>11. (a) <math>36 - (20 + a) = 14</math><br/> <math>a = 2</math><br/><br/> <math>30 + b = 31</math><br/> <math>b = 1</math></p>                                                                                                                                                                                                                                                                                                                                                                               | <p>1M<br/>1A<br/><br/>1A</p> <p>----- (3)</p> |                                                                                 |
| <p>(b) (i) The original mode<br/> <math>= 36</math><br/><br/>           The new mode<br/> <math>= 36</math><br/><br/>           Thus, there is no change in the mode of the distribution.</p>                                                                                                                                                                                                                                                                                                                   | <p>1M<br/><br/><br/>1A</p>                    | <p>-----<br/>           either one<br/>           -----<br/>           f.t.</p> |
| <p>(ii) There are two cases.<br/><br/>           Case 1: The player of age 17 leaves the football team.<br/><br/>           The standard deviation of the distribution<br/> <math>\approx 7.162537194</math><br/><br/>           Case 2: The player of age 43 leaves the football team.<br/><br/>           The standard deviation of the distribution<br/> <math>\approx 7.132307207</math><br/><br/>           Thus, the greatest possible standard deviation of the distribution<br/>           is 7.16.</p> | <p>1M<br/><br/><br/>1A</p> <p>----- (4)</p>   | <p>-----<br/>           either one<br/>           -----<br/>           f.t.</p> |

| Solution                                                                                                                                                                                                                                                                                                                                                | Marks                                                    | Remarks |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------|---------|
| <p>12. (a) The coordinates of <math>G</math></p> $= \left( \frac{154}{2}, \frac{128}{2} \right)$ $= (77, 64)$ <p>The distance between <math>G</math> and <math>H</math></p> $= \sqrt{(77 - 65)^2 + (64 - 48)^2}$ $= 20$                                                                                                                                 | <p>1M</p> <p>1M</p> <p>1A</p> <p>----- (3)</p>           |         |
| <p>(b) (i) <math>GH</math> is perpendicular to <math>GP</math>.</p> <p>(ii) The radius of <math>C</math></p> $= \sqrt{\left( \frac{154}{2} \right)^2 + \left( \frac{128}{2} \right)^2} - 224$ $= 99$ $HP^2 = GH^2 + GP^2$ $HP^2 = 20^2 + 99^2$ $HP = 101$ <p>The perimeter of <math>\triangle GHP</math></p> $= GH + GP + HP$ $= 20 + 99 + 101$ $= 220$ | <p>1M</p> <p>1M</p> <p>1M</p> <p>1A</p> <p>----- (4)</p> |         |

| Solution                                                                                                                                                                                                               | Marks                  | Remarks    |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------|------------|
| 13. (a) The ratio of the volume of the smaller sphere to the volume of the larger sphere is $8 : 27$ .<br>The volume of the smaller sphere<br>$= \frac{4}{3}\pi(9)^3\left(\frac{8}{27}\right)$ $= 288\pi \text{ cm}^3$ | 1M<br><br>1M<br><br>1A |            |
|                                                                                                                                                                                                                        | ----- (3)              |            |
| (b) The volume of $A$<br>$= \frac{1}{3}\pi(6^2)(10)$ $= 120\pi \text{ cm}^3$                                                                                                                                           | 1M                     |            |
| The volume of $B$<br>$= 288\pi + \frac{4}{3}\pi(9)^3 - 120\pi$ $= 1140\pi \text{ cm}^3$                                                                                                                                | 1M                     |            |
| $\frac{\text{The volume of } B}{\text{The volume of } A}$ $= \frac{1140\pi}{120\pi}$ $= \frac{19}{2}$                                                                                                                  | 1M                     |            |
| $\left(\frac{\text{The base radius of } B}{\text{The base radius of } A}\right)^3$ $= \left(\frac{12}{6}\right)^3$ $= 8$ $\neq \frac{19}{2}$                                                                           |                        | either one |
| So, $A$ and $B$ are not similar.<br>Thus, the claim is not correct.                                                                                                                                                    | 1A                     | f.t.       |
|                                                                                                                                                                                                                        | ----- (4)              |            |

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| Solution                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | Marks                                          | Remarks                                       |
|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------|-----------------------------------------------|
| <p>14. (a) Let <math>p(x) = (mx + n)(x^2 - 2x + 3) + x + 13</math>, where <math>m</math> and <math>n</math> are constants.</p> <p>Therefore, we have <math>p(x) = mx^3 + (n - 2m)x^2 + (3m - 2n + 1)x + 3n + 13</math>.</p> <p>So, we have <math>m = 2</math> and <math>3n + 13 = -20</math>.</p> <p>Solving, we have <math>m = 2</math> and <math>n = -11</math>.</p> <p>Hence, we have <math>p(x) = 2x^3 - 15x^2 + 29x - 20</math>.</p> <p>Thus, we have <math>a = -15</math> and <math>b = 29</math>.</p>                                                                                 | <p>1M</p> <p>1M</p> <p>1A</p> <p>----- (3)</p> | <p>for either one</p> <p>for both correct</p> |
| <p>(b) <math>p(5)</math></p> <p><math>= 2(5)^3 - 15(5)^2 + 29(5) - 20</math></p> <p><math>= 0</math></p> <p>Thus, <math>x - 5</math> is a factor of <math>p(x)</math>.</p>                                                                                                                                                                                                                                                                                                                                                                                                                   | <p>1M</p> <p>1A</p> <p>----- (2)</p>           | <p>f.t.</p>                                   |
| <p>(c) <math>p(x) = 0</math></p> <p><math>(x - 5)(2x^2 - 5x + 4) = 0</math></p> <p><math>x - 5 = 0</math> or <math>2x^2 - 5x + 4 = 0</math></p> <p><math>(-5)^2 - 4(2)(4)</math></p> <p><math>= -7</math></p> <p><math>&lt; 0</math></p> <p>So, the quadratic equation <math>2x^2 - 5x + 4 = 0</math> has no real roots.</p> <p>Hence, the quadratic equation <math>2x^2 - 5x + 4 = 0</math> has no irrational roots.</p> <p>Note that 5 is not an irrational number.</p> <p>Therefore, the equation <math>p(x) = 0</math> has no irrational roots.</p> <p>Thus, the claim is disagreed.</p> | <p>1M</p> <p>1M</p> <p>1A</p> <p>----- (3)</p> | <p>f.t.</p>                                   |

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| Solution                                                                                                                                                                                                                                                                           | Marks                         | Remarks                                                         |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------|-----------------------------------------------------------------|
| <p>15. (a) The required probability</p> $= \frac{C_2^{10} C_2^{12}}{C_4^{22}}$ $= \frac{54}{133}$                                                                                                                                                                                  | <p>1M</p> <p>1A</p>           | <p>for numerator</p> <p>r.t. 0.406</p>                          |
| <p>The required probability</p> $= 6 \left( \frac{10}{22} \right) \left( \frac{9}{21} \right) \left( \frac{12}{20} \right) \left( \frac{11}{19} \right)$ $= \frac{54}{133}$                                                                                                        | <p>1M</p> <p>1A</p>           | <p>for <math>6p_1 p_2 p_3 p_4</math></p> <p>r.t. 0.406</p>      |
|                                                                                                                                                                                                                                                                                    | ----- (2)                     |                                                                 |
| <p>(b) The required probability</p> $= 1 - \frac{54}{133}$ $= \frac{79}{133}$                                                                                                                                                                                                      | <p>1M</p> <p>1A</p>           | <p>for <math>1 - (a)</math></p> <p>r.t. 0.594</p>               |
| <p>The required probability</p> $= \frac{C_4^{10}}{C_4^{22}} + \frac{C_3^{10} C_1^{12}}{C_4^{22}} + \frac{C_1^{10} C_3^{12}}{C_4^{22}} + \frac{C_4^{12}}{C_4^{22}}$ $= \frac{79}{133}$                                                                                             | <p>1M</p> <p>1A</p>           | <p>for <math>p_5 + p_6 + p_7 + p_8</math></p> <p>r.t. 0.594</p> |
|                                                                                                                                                                                                                                                                                    | ----- (2)                     |                                                                 |
| <p>16. (a) <math>g(x)</math></p> $= 3x^2 + 12kx + 16k^2 + 8$ $= 3(x^2 + 4kx) + 16k^2 + 8$ $= 3(x^2 + 4kx + 4k^2) + 4k^2 + 8$ $= 3(x + 2k)^2 + 4k^2 + 8$ <p>Thus, the coordinates of the vertex are <math>(-2k, 4k^2 + 8)</math>.</p>                                               | <p>1M</p> <p>1A</p>           | <p>----- (2)</p>                                                |
| <p>(b) The coordinates of <math>B</math> are <math>(2k, 8k^2 + 16)</math>.</p> <p>Note that <math>AM : MB = 1 : 3</math>.</p> <p>The coordinates of <math>M</math></p> $= \left( \frac{3(-2k) + (2k)}{1 + 3}, \frac{3(4k^2 + 8) + (8k^2 + 16)}{1 + 3} \right)$ $= (-k, 5k^2 + 10)$ | <p>1M</p> <p>1M</p> <p>1A</p> | <p>----- (3)</p>                                                |

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| Solution                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | Marks                                                   | Remarks        |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------|----------------|
| 17. (a) Note that $\alpha + \beta = -c$ and $\alpha\beta = -9$ .<br>$\alpha^2 + \beta^2$ $= (\alpha + \beta)^2 - 2\alpha\beta$ $= (-c)^2 - 2(-9)$ $= c^2 + 18$                                                                                                                                                                                                                                                                                                                                                               | 1M<br><br>1M<br><br>1A<br>----- (3)                     | for either one |
| (b) $\alpha^2 + \beta^2 - c^2 = 85 - (\alpha^2 + \beta^2)$<br>$c^2 + 18 - c^2 = 85 - (c^2 + 18)$<br>$c^2 = 49$<br><br>Note that the 1st term and the common difference of the sequence are 49 and 18 respectively.<br>$\frac{n}{2}(2(49) + 18(n-1)) > 2 \times 10^6$ $9n^2 + 40n - 2 \times 10^6 > 0$ $n < \frac{-40 - \sqrt{40^2 - 4(9)(-2 \times 10^6)}}{2(9)} \text{ or } n > \frac{-40 + \sqrt{40^2 - 4(9)(-2 \times 10^6)}}{2(9)}$ $n < -473.6319808 \text{ or } n > 469.1875364$ Thus, the least value of $n$ is 470 . | 1M<br><br><br><br><br><br><br>1M<br><br>1A<br>----- (4) |                |

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| Solution                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | Marks                                          | Remarks                                                                                                                                                         |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <p>19. (a) The slope of <math>AG</math></p> $= \frac{112 - 12}{83 - 158}$ $= \frac{-4}{3}$ <p>The required equation is</p> $y - 12 = \frac{-4}{3}(x - 158)$ $4x + 3y - 668 = 0$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | <p>1M</p> <p>1A</p> <p>----- (2)</p>           | <p>or equivalent</p>                                                                                                                                            |
| <p>(b) The radius of <math>C</math> is 75 .</p> <p>Since <math>83 + 75 = 158</math> , <math>AP</math> is vertical or <math>AQ</math> is vertical.</p> <p>So, the coordinates of <math>P</math> or the coordinates of <math>Q</math> are <math>(158, 112)</math> .</p> <p>Note that <math>\triangle AGP \cong \triangle AGQ</math> and <math>AG \perp PQ</math> .</p> <p>Hence, the slope of <math>PQ</math> is <math>\frac{3}{4}</math> .</p> <p>The equation of <math>PQ</math> is <math>y - 112 = \frac{3}{4}(x - 158)</math> .</p> <p>Solving <math>y - 112 = \frac{3}{4}(x - 158)</math> and <math>4x + 3y - 668 = 0</math> , we have</p> $x = 110 \text{ and } y = 76 .$ <p>Thus, the coordinates of the point of intersection of <math>AG</math> and <math>PQ</math> are <math>(110, 76)</math> .</p>                                                                                                                                                                                                                                                                                             | <p>1M</p> <p>1M</p> <p>1A</p> <p>----- (3)</p> |                                                                                                                                                                 |
| <p>(c) Let <math>I</math> and <math>r</math> be the centre and the radius of the inscribed circle of <math>\triangle APQ</math> respectively.</p> <p>Note that <math>AP = AQ</math> and <math>I</math> lies on <math>AG</math> .</p> <p>The <math>x</math>-coordinate of <math>I</math></p> $= 158 - r$ <p>The <math>y</math>-coordinate of <math>I</math></p> $= \frac{-4}{3}(158 - r) + \frac{668}{3}$ $= \frac{4r}{3} + 12$ <p>So, the coordinates of <math>I</math> are <math>\left(158 - r, \frac{4r}{3} + 12\right)</math> .</p> <p>The distance between <math>I</math> and the point of intersection of <math>AG</math> and <math>PQ</math> is <math>r</math> .</p> $((158 - r) - 110)^2 + \left(\left(\frac{4r}{3} + 12\right) - 76\right)^2 = r^2$ $\frac{16}{9}r^2 - \frac{800}{3}r + 6\,400 = 0$ $r^2 - 150r + 3\,600 = 0$ $r = 30 \text{ or } r = 120 \text{ (rejected)}$ <p>Therefore, we have <math>r = 30</math> .</p> <p>Hence, the coordinates of <math>I</math> are <math>(128, 52)</math> .</p> <p>Thus, the required equation is <math>(x - 128)^2 + (y - 52)^2 = 30^2</math> .</p> | <p>1M</p> <p>1M</p> <p>1A</p> <p>----- (4)</p> | <p>accept <math>110 + \frac{3r}{5}</math></p> <p>accept <math>158 - r = 110 + \frac{3r}{5}</math></p> <p><math>x^2 + y^2 - 256x - 104y + 18\,188 = 0</math></p> |

| Solution                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             | Marks                                       | Remarks     |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------|-------------|
| <p>(d) Note that <math>\angle APG = \angle AQG = 90^\circ</math> and <math>\angle APG + \angle AQG = 180^\circ</math> .<br/>           So, <math>APGQ</math> is a cyclic quadrilateral and <math>AG</math> is a diameter of the circumcircle of <math>\triangle APQ</math> .<br/>           The radius of the circumcircle of <math>\triangle APQ</math><br/> <math display="block">= \frac{1}{2} \sqrt{(83-158)^2 + (112-12)^2}</math> <math display="block">= \frac{125}{2}</math></p> <p>By (c), the radius of the inscribed circle of <math>\triangle APQ</math> is 30 .</p> <p>The ratio of the area of the inscribed circle to the area of the circumcircle of <math>\triangle APQ</math><br/> <math display="block">= 30^2 : \left(\frac{125}{2}\right)^2</math> <math display="block">= 144 : 625</math> <math display="block">\neq 1 : 4</math>           Thus, the claim is disagreed.</p> | <p>1M</p> <p>1M</p> <p>1A<br/>----- (3)</p> | <p>f.t.</p> |

Paper 2

Since 1996

| MC answer |   |   |   |   |   |   |   |   |    |
|-----------|---|---|---|---|---|---|---|---|----|
| 1         | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| D         | B | A | D | A | B | A | B | D | A  |
| C         | C | B | C | A | D | B | C | D | B  |
| B         | C | C | A | D | A | C | D | A | B  |
| C         | C | D | A | B | B | D | D | C | A  |
| A         | B | B | C | D |   |   |   |   |    |